

**PANDIAN SARASWATHI YADAV ENGINEERING COLLEGE**

**MA6459- NUMERICAL METHODS**

**PART-B QUESTIONS**

**UNIT – I**

**SOLUTION OF EQUATIONS AND EIGENVALUE PROBLEMS**

1. Find the positive root of  $x^4 - x = 10$  correct to three decimal places using Newton – Raphson method. [A.U MAY 1996, A.U A/M 2010]
2. Using Newton iterative method find the root between 0 & 1 of  $x^3 = 6x - 4$  correct to two places. [A.U MAY 2000, A.U M/J 2008]
3. Find the real positive root of  $3x - \cos x - 1 = 0$  by newton method correct to 6 decimal places. [A.U 2015, A.U M/J 2007, N/D 2009]
4. Find a root of  $x \log_{10} x - 1.2 = 0$  by N – R method correct to 3 decimal places. [A.U N/D 2015, M/J 2007, M/J 2010, N/D 2010]
5. Obtain newton iterative formula for finding root N . where N is a positive real number. Hence evaluate root of 142. [A.U MAY 1999]
6. Solve the following system of equations by Gauss – Jordan method.  
 $10x+y+z = 12, 2x+10y+z = 13, x+y+5z = 7$  [A.U A/M 2008, M/J 2010, N/D 2014]
7. Solve the following system of equations by Gauss – Jacobi method.  
 $27x+6y-z = 85, x+y+54z = 110, 6x+15y+2z = 72$  [A.U A/M 2009, M/J 2006, M/J 2010]
8. Solve the following system of equations by Gauss – Jacobi Gauss – Seidel method.  
 $20x+y-2z = 17, 3x+20y-z = -18, 2x-3y+20z = 25$  [A.U M/J 2009, N/D 2009]
9. Using Gauss – Jordan method, find the inverse of  $A = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{pmatrix}$  [A.U N/D 2004, APL 2000, OCT 1996]
10. Find the dominant eigen value and the corresponding eigen vector of  $A = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{pmatrix}$ . Find also the least latent root and hence the third eigen value also. [A.U M/J 2010, M/J 2007, A/M 2008, A/M 2010]

11. Find the numerically largest eigen value of  $A = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$  and the corresponding eigen

vector

[A.U M/J 2006, A/M 2008]

12. Apply Jacobi process to evaluate the eigen values and eigen vectors of the

matrix  $A = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$

[A.U A/M 2015]

## UNIT – II

### INTERPOLATION AND APPROXIMATION

1. Find the polynomial  $f(x)$  by using Lagrange's formula and hence find  $f(3)$  for

x	0	1	2	5
f(x)	2	3	12	147

[A.U A/M 2008]

2. Using Lagrange's interpolation, calculate the profit in the year 2000 from the

following data:

[A.U A/M 2011]

Year:	1997	1999	2001	2002
Profit in lakhs of Rs.	43	65	159	248

[A.U A/M 2014]

3. Find the missing term in the following table using Lagrange's interpolation.

x	0	1	2	3	4
y	1	3	9	-	81

[A.U A/M 2011]

4. Find the lagrangian interpolating polynomial for the following data:

x	1	2	3	5
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$f(x)$	0	7	26	124
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[A.U 2010, M/J 2010]

5. Using Newton's divided difference formula, find  $u(3)$  given  $u(1) = -26$ ,  $u(2) = 12$ ,

$u(4) = 256$ ,  $u(6) = 844$ .

[A.U A/M 2004]

6. Find  $f(x)$  as a polynomial in  $x$  for the following data by Newton's divided difference formula

$x$	-4	-1	0	2	5
$f(x)$	1245	33	5	9	1335

[A.U N/D 2013]

7. Find the missing term in the following table using divided difference .

$x$	1	2	4	5	6
$y$	14	15	5	-	9

[A.U A/M 2012]

8. Obtain the cubic spline approximation for the function  $y = f(x)$  from the following data, given that  $y_0'' = y_3'' = 0$ .

$x$	-1	0	1	2
$f(x)$	-1	1	3	35

[A.U M/J 2010, N/D 2010,2011]

9. Using Newton's forward interpolation formula, find the polynomial  $f(x)$  satisfying the following data. Hence evaluate  $y$  at  $x = 5$ .

$x$	4	6	8	10
$y$	1	3	8	10

[A.U A/M 2014]

10. Use Newton's backward difference formula to construct an interpolating polynomial of degree 3 for the data:  $f(-0.75) = -0.07181250$ ,  $f(-0.5) = -0.024750$ ,

$f(-0.25) = -0.33493750$ ,  $f(0) = 1.10100$ . Hence find  $f(-1/3)$

[A.U A/M 2013]

11. From the following data, find  $\Theta$  at  $x = 43$  and  $x = 84$

x	40	50	60	70	80	90
$\Theta$	184	204	226	250	276	304

[A.U N/D 2010,2011]

12. From the data given below, find the number of students whose weight is between 60 to 70.

Weight in lbs:	0-40	40-60	60-80	80-100	100-120
No. of students	250	120	100	70	50

[A.U N/D 2003, A/M 2010,2011,2012]

13. The following data are taken from the table:

Temp. $^{\circ}\text{C}$ :	140	150	160	170	180
Pressure $\text{kgf/cm}^2$	3.685	4.854	6.302	8.076	10.225

[A.U M/J 2009, N/D 2010]

### UNIT-III

#### NUMERICAL DIFFERENTIATION AND INTEGRATION

1. Given data

(A.U M/J 2015)

X	1.0	1.1	1.2	1.3	1.4	1.5	1.6
F(x)	7.989	8.403	8.781	9.129	9.451	9.750	10.031

Find  $\frac{dy}{dx}$  at  $x=1.1$

2. Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  at  $x=1.5$  from the following data

(A.U M/J 2015)

X:	1.5	2	2.5	3	3.5	4
Y:	3.375	7	13.625	24	38.875	59

3. Find  $y'$  at  $x=51$  from the following data

(A.U M/J 2015, 2014, 2013)

X:	50	60	70	80	90
Y:	19.96	36.65	58.81	77.21	94.61

4. Find  $y'$  at  $x=51$  from the following data

(A.U M/J 2015, 2014, 2013, 2012)

X:	50	60	70	80	90
Y:	19.96	36.65	58.81	77.21	94.61

5. The following data gives the velocity of a particle for 20 seconds at an interval of 5 seconds. Find the initial acceleration using the entire data. (A.U M/J 2013)

Time(sec)	0	5	10	15	20
Velocity(m/sec)	0	3	14	69	228

6. Using Romberg's rule evaluate  $I = \int_0^1 \frac{dx}{1+x}$  correct to three decimal places by taking

$h = 0.5, 0.25$  and  $0.125$ .

(A.U M/J 2014, 2015)

9. Evaluate  $\int_0^{\pi/2} \sin x dx$  using (i) Simpson's  $\frac{1}{3}$ <sup>rd</sup> rule and (ii) Simpson's  $\frac{3}{8}$ <sup>th</sup> rule, by dividing the range into six equal subintervals. (A.U M/J 2014, 2013)

10. Evaluate  $\int_0^1 \frac{dx}{1+x^2}$  by using Simpson's  $\frac{3}{8}$  rule, dividing the range into 6 equal parts (h=0.2). (A.U M/J 2014, 2012)

11. Evaluate  $\int_0^2 \int_0^1 4xy dx dy$  by using Simpson's rule and taking  $h = \frac{1}{4}$  and  $k = \frac{1}{2}$  (M/J 2012)

12. Evaluate  $\int_{2.4}^{2.44} \int_{.4}^{.44} xy dx dy$  using Simpson's rule (h = k = 0.1). (M/J 2013)

#### UNIT-IV

##### INITIAL VALUE PROBLEMS FOR ORDINARY DIFFERENTIAL EQUATIONS

1. Solve  $\frac{dy}{dx} = x^2 + y^2$ ,  $y(0) = 1$ , Use Taylor series method at  $x = 0.2$ , and  $0.4$ . (A.U 2015)

2. Using Runge –Kutta method of fourth order, solve  $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$  with  $y(0)=1$  at  $x=0.2$  (A.U 2015,2014,2011)

3. Given  $\frac{dy}{dx} = xy + y^2$ ,  $y(0)=1$ ,  $y(0.1)=1.1169$  and  $y(0.2)=1.2774$  find (i)  $y(0.3)$  by R.K method of fourth order and (ii)  $y(0.4)$  by Milne's method. (A.U 2015,2014,2013,2011)

4. Solve the equation  $\frac{dy}{dx} = 1 - y$ , given  $y(0) = 0$  using modified Euler method and tabulate the solution at  $x = 0.1, 0.2$  and  $0.3$ . hence find  $y(0.4)$  by Milne's method.

(A.U 2015,2014,2013,2011)

5. Apply Milne's method, to find a solution of the differential equation  $\frac{dy}{dx} = x - y^2$  at  $x = 0.8$ , given the values. Use Taylor series method to find  $y(0.1)$ ,  $y(0.2)$  and  $y(0.3)$ . (A.U, 2013, 2011)

6. Using R.K method, solve  $y'' = y + xy'$ ,  $y(0) = 1$ ,  $y'(0) = 0$  to find  $y(0.2)$  and  $y'(0.2)$ . (A.U 2015, 2014, 2013, 2010)

7. Consider the initial value problem  $\frac{dy}{dx} = y - x^2 + 1$ ,  $y(0) = 0.5$  (A.U 2015, 2014, 2013, 2011)

(i) Using the modified Euler's Method, find  $y(0.2)$

(ii) Using 4<sup>th</sup> order R-K method find  $y(0.4)$  and  $y(0)$ .

(iii) Using Adam's Bashforth Method to find  $y(0.8)$

## UNIT- V

### **BOUNDARY VALUE PROBLEMS IN ORDINARY AND PARTIAL DIFFERENTIAL EQUATIONS**

1. Obtain the Crank-Nicholson finite difference method by taking  $\lambda = \frac{kc^2}{h^2} = 1$ . Hence find  $u(x, t)$

in the root for two times steps for the heat equation  $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ , given

$u(x, 0) = \sin(\pi x)$ ,  $u(0, t) = u(1, t) = 0$ . Take  $h = 0.2$ .

(A.U 2015, 2013)

2. Solve  $\nabla^2 u = 8x^2 y^2$  in the square region  $-2 \leq x, y \leq 2$  with  $u=0$  on the boundaries after

dividing the region into 16 sub intervals of length one unit.

(A.U 2015, 2013)

3. Evaluate  $u(x, t)$  at the pivotal points of the equation  $\frac{\partial u}{\partial t} = 16 \frac{\partial^2 u}{\partial x^2}$ ,  $\frac{\partial u}{\partial t}(x, 0)$

$= 0$ ,  $u(0, t) = 0$ ,  $u(5, t) = 0$ , and  $u(x, 0) = x^2(5-x)$  taking  $\Delta x = 1$  and upto  $t = 1.25$ .

(A.U 2012)

4. Solve  $u_t = u_{xx}$  in  $0 < x < 5$ ,  $t > 0$  given that  $U(x,0) = x^2(25-x^2)$ ,  $U(0,t)=0=U(5,t)$ . compute  $u$  upto  $t=2$  with  $\Delta x = 1$  by using Bender Smith formula. (A.U 2013)

5. Use Crank Nicholson scheme to solve  $\frac{\partial u}{\partial t} = 16 \frac{\partial^2 u}{\partial x^2}$ ,  $0 < x < 1$  and  $t > 0$  given  $u(x,0)=0, u(0,t)=0$ , and  $u(1,t)=100t$ . Compute  $u(x,t)$  for one time step taking  $\Delta x=1/4$ . (A.U 2015,2014,2011)

6. Deduce the standard five point formula for  $\nabla^2 u = 0$  hence solve it over the square region given by the boundary conditions as in figure below (A.U 2012,2011,2010)

	$u_1$	$u_2$
	$u_3$	$u_4$

7. Solve  $\frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2}$ ,  $0 < x < 1$ ,  $t > 0$  given

$u(x,0)=0$ ,  $\frac{\partial u}{\partial t}(x,0) = 0$ ,  $u(0,t)=0$  and  $u(1,t)=100 \sin \pi t$ . Compute  $u(x,t)$  for the four time steps with  $h=0.25$ . (A.U 2013,2011)

8. Solve the boundary value problem  $y'' = xy$  subject to the condition  $y(0)+y'(0)=1$ ,  $y(1)=1$  taking  $h=1/3$  by finite difference method. (A.U 2014,2010)

\*\*\*\*\* *ALL THE BEST* \*\*\*\*\*